

Model Question Paper-I with effect from 2022

USN

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Fourth Semester B.E Degree Examination

Complex Analysis, Probability & Statistical Methods

All branches Except CS & ME Engg.Allied branches-21MAT41

TIME: 03 Hours
Max. Marks: 100

Note: Answer any **FIVE** full questions, choosing at least **ONE** question from each module.

Q.No.	Question	M	L	CO																	
Module -1																					
01	a	Define analytic function and derive C-R equations in Cartesian form.	06	L2	CO1																
	b	Show that $f(z) = \log z$ is analytic and hence obtain its derivative.	07	L2	CO1																
	c	Evaluate $\int_0^{1+i} (x^2 - iy) dz$ along the curve $y = x^2$.	07	L3	CO1																
OR																					
02	a	Construct an analytic function, whose imaginary part is $v = e^x(x \sin y + y \cos y)$ by the Milne-Thomson method	06	L2	CO1																
	b	State and prove Cauchy's integral formula.	07	L2	CO1																
	c	Evaluate $\int_C \frac{\sin \pi z^2 + \cos \pi z^2}{(z-1)(z-2)} dz$, where $C: z = 3$.	07	L3	CO1																
Module-2																					
03	a	Obtain the series solution of Bessel's differential equation $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + (x^2 + n^2)y = 0$	06	L2	CO2																
	b	Show that $J_{\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \sin x$.	07	L2	CO2																
	c	Express $x^3 - 5x^2 + 6x + 1$ in terms of Legendre polynomial	07	L2	CO2																
OR																					
4	a	Show that $J_{-n}(x) = (-1)^n J_n(x)$		L2	CO2																
	b	Show that $P_4(\cos \theta) = \frac{1}{64} (35 \cos 4\theta + 2\theta \cos \theta + 9)$.	07	L2	CO2																
	c	Prove that $x^3 - 2x^2 - x - 3 = \frac{2}{5} P_3(x) + \frac{4}{3} P_2(x) - \frac{2}{5} P_1(x) - \frac{7}{3} P_0(x)$	07	L2	CO2																
Module-3																					
5	a	Find Karl Pearson's coefficient of correlation. <table border="1" style="margin: 10px auto; border-collapse: collapse;"> <tr> <td style="padding: 2px 10px;">x:</td> <td style="padding: 2px 10px;">1</td> <td style="padding: 2px 10px;">2</td> <td style="padding: 2px 10px;">3</td> <td style="padding: 2px 10px;">4</td> <td style="padding: 2px 10px;">5</td> <td style="padding: 2px 10px;">6</td> <td style="padding: 2px 10px;">7</td> </tr> <tr> <td style="padding: 2px 10px;">y:</td> <td style="padding: 2px 10px;">9</td> <td style="padding: 2px 10px;">8</td> <td style="padding: 2px 10px;">10</td> <td style="padding: 2px 10px;">12</td> <td style="padding: 2px 10px;">11</td> <td style="padding: 2px 10px;">13</td> <td style="padding: 2px 10px;">14</td> </tr> </table>	x:	1	2	3	4	5	6	7	y:	9	8	10	12	11	13	14	06	L2	CO3
x:	1	2	3	4	5	6	7														
y:	9	8	10	12	11	13	14														

b	Fit a straight line $y = ax + b$ for the data	07	L2	CO3											
	<table border="1"> <tr> <td>x:</td> <td>5</td> <td>10</td> <td>15</td> <td>20</td> <td>25</td> </tr> <tr> <td>y:</td> <td>16</td> <td>19</td> <td>23</td> <td>26</td> <td>30</td> </tr> </table>	x:	5	10	15	20	25	y:	16	19	23	26	30		
x:	5	10	15	20	25										
y:	16	19	23	26	30										
c	Find the regression lines of y on x and x on y for the following data	07	L2	CO3											
	<table border="1"> <tr> <td>x:</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>y:</td> <td>2</td> <td>5</td> <td>3</td> <td>8</td> <td>7</td> </tr> </table>	x:	1	2	3	4	5	y:	2	5	3	8	7		
x:	1	2	3	4	5										
y:	2	5	3	8	7										

OR

6	a	The participants in a contest are ranked by two judges as follows.	06	L2	CO3																						
		<table border="1"> <tr> <td>x:</td> <td>1</td> <td>6</td> <td>5</td> <td>10</td> <td>3</td> <td>2</td> <td>4</td> <td>9</td> <td>7</td> <td>8</td> </tr> <tr> <td>y:</td> <td>6</td> <td>4</td> <td>9</td> <td>8</td> <td>1</td> <td>2</td> <td>3</td> <td>10</td> <td>5</td> <td>7</td> </tr> </table> <p>Compute the Rank correlation.</p>	x:	1	6	5	10	3	2	4	9	7	8	y:	6	4	9	8	1	2	3	10	5	7			
x:	1	6	5	10	3	2	4	9	7	8																	
y:	6	4	9	8	1	2	3	10	5	7																	
	b	Compute means \bar{x} , \bar{y} and the correlation coefficient r from the given regression lines $2x + 3y + 1 = 0$, $x + 6y = 4$.	07	L2	CO3																						
	c	Fit a second degree polynomial $y = ax^2 + bx + c$ for the data.	07	L2	CO3																						
		<table border="1"> <tr> <td>x:</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>y:</td> <td>10</td> <td>12</td> <td>13</td> <td>16</td> <td>19</td> </tr> </table>	x:	1	2	3	4	5	y:	10	12	13	16	19													
x:	1	2	3	4	5																						
y:	10	12	13	16	19																						

Module-4

7	a	A random variable X has the following probability function:	06	L2	CO4															
		<table border="1"> <tr> <td>X</td> <td>-3</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> </tr> <tr> <td>P(X)</td> <td>k</td> <td>2k</td> <td>3k</td> <td>4k</td> <td>3k</td> <td>2k</td> <td>k</td> </tr> </table> <p>Find k. Also find $P(X \leq 1)$, $P(X > 1)$, $P(-1 < X \leq 2)$,</p>	X	-3	-2	-1	0	1	2	3	P(X)	k	2k	3k	4k	3k	2k	k		
X	-3	-2	-1	0	1	2	3													
P(X)	k	2k	3k	4k	3k	2k	k													
	b	Find the mean and variance of Binomial distribution.	07	L2	CO4															
	c	In a certain factory turning out razor blades there is a small probability of $\frac{1}{500}$ for any blade to be defective. The blades are supplied in a packets of 10. Use Poisson distribution to calculate approximate number of packets containing i) No defective ii) Two defective iii) Three defective in consignment of 10000 packets.	07	L3	CO4															

OR

8	a	A random variable X has density function: $f(x) = \begin{cases} kx^2 & -3 \leq x \leq 3 \\ 0 & \text{Otherwise} \end{cases}$ Find k . Also, find $P(X \leq 2)$, $P(X \geq 2)$ and $P(X > 1)$.	06	L2	CO4
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b	The probability that a pen manufactured by a company will be defective is 0.1. If 12 such pens are selected at random, find the probability that i) Exactly two pens will be defective ii) At most two pens will be defective iii) None will be defective	07	L2	CO4
c	The marks of 1000 students in an examination follow the normal distribution with mean 70 and standard deviation 5. Find the number students whose marks will be i) Less than 65 ii) More than 75 iii) Between 65 and 75.	07	L3	CO4

Module-5

9	a	The joint distribution of two random variables X and Y is as follows. <table border="1" style="margin: 10px auto;"> <tr> <td style="border: none;"></td> <td style="border: none;">Y</td> <td style="border: none;"></td> <td style="border: none;"></td> <td style="border: none;"></td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;">X</td> <td style="border: none;"></td> <td style="border: none;"></td> <td style="border: none;"></td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;"></td> <td style="border: none;">-4</td> <td style="border: none;">2</td> <td style="border: none;">7</td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;">1</td> <td style="border: none;">$\frac{1}{8}$</td> <td style="border: none;">$\frac{1}{4}$</td> <td style="border: none;">$\frac{1}{8}$</td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;">5</td> <td style="border: none;">$\frac{1}{4}$</td> <td style="border: none;">$\frac{1}{8}$</td> <td style="border: none;">$\frac{1}{8}$</td> </tr> </table> <p>Compute the following. i) $E(X)$ and $E(Y)$ ii) $E(XY)$ iii) σ_x & σ_y</p>		Y					X						-4	2	7		1	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$		5	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{8}$	06	L2	CO5
	Y																													
	X																													
		-4	2	7																										
	1	$\frac{1}{8}$	$\frac{1}{4}$	$\frac{1}{8}$																										
	5	$\frac{1}{4}$	$\frac{1}{8}$	$\frac{1}{8}$																										
b	Define i) Null hypothesis ii) Type-I & Type-II errors iii) Degrees of freedom iv) Level of Significance.	07	L2	CO5																										
c	Two types of batteries are tested for their length of life and the following results are obtained: Battery A: $n_1 = 10$ $\bar{x}_1 = 500$ Hrs. $\sigma_1^2 = 100$ Battery B: $n_2 = 10$ $\bar{x}_2 = 506$ Hrs. $\sigma_2^2 = 121$ Compute Student's t and test whether there is a significant difference in the two means at 5% significance level.	07	L3	CO5																										

OR

10	a	Determine (i) Marginal distributions (ii) Covariance between the variables X and Y, If the joint probability distribution is given by: <table border="1" style="margin: 10px auto;"> <tr> <td style="border: none;"></td> <td style="border: none;">Y</td> <td style="border: none;"></td> <td style="border: none;"></td> <td style="border: none;"></td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;">X</td> <td style="border: none;"></td> <td style="border: none;"></td> <td style="border: none;"></td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;"></td> <td style="border: none;">3</td> <td style="border: none;">4</td> <td style="border: none;">5</td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;">2</td> <td style="border: none;">$\frac{1}{6}$</td> <td style="border: none;">$\frac{1}{6}$</td> <td style="border: none;">$\frac{1}{6}$</td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;">5</td> <td style="border: none;">$\frac{1}{12}$</td> <td style="border: none;">$\frac{1}{12}$</td> <td style="border: none;">$\frac{1}{12}$</td> </tr> <tr> <td style="border: none;"></td> <td style="border: none;">7</td> <td style="border: none;">$\frac{1}{12}$</td> <td style="border: none;">$\frac{1}{12}$</td> <td style="border: none;">$\frac{1}{12}$</td> </tr> </table>		Y					X						3	4	5		2	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$		5	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$		7	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$	06	L2	CO5
	Y																																		
	X																																		
		3	4	5																															
	2	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$																															
	5	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$																															
	7	$\frac{1}{12}$	$\frac{1}{12}$	$\frac{1}{12}$																															

b	Ten individuals are chosen at random from a population and their heights in inches are found to be 63, 63, 66, 67, 68, 69, 70, 70, 71, 71. Test the hypothesis that the mean height of the universe is 66 inches at 5% significance level. ($t_{0.05} = 2.262$ for 9 d.f.)	07	L3	CO5										
c	<p>In experiments on pea breeding the following frequencies of seeds were obtained:</p> <table border="1" data-bbox="175 373 1253 485"> <tr> <td>Round and Yellow</td> <td>Wrinkled and Yellow</td> <td>Round and Green</td> <td>Wrinkled and Green</td> <td>Total</td> </tr> <tr> <td>315</td> <td>101</td> <td>108</td> <td>32</td> <td>556</td> </tr> </table> <p>Theory predicts that the frequencies should be in proportions 9: 3: 3: 1. Examine the correspondence between theory and experiment</p>	Round and Yellow	Wrinkled and Yellow	Round and Green	Wrinkled and Green	Total	315	101	108	32	556	07	L3	CO5
Round and Yellow	Wrinkled and Yellow	Round and Green	Wrinkled and Green	Total										
315	101	108	32	556										

Bloom's Taxonomy Levels	Lower-order thinking skills		
	Remembering (knowledge):L ₁	Understanding (Comprehension): L ₂	Applying (Application):L ₃
	Higher-order thinking skills		
	Analyzing (Analysis):L ₄	Valuating (Evaluation): L ₅	Creating (Synthesis): L ₆

USN

Model Question Paper-II with effect from 2022

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Fourth Semester B.E Degree Examination

Complex Analysis, Probability & Statistical Methods

All branches Except CS & ME Engg. Allied branches-21MAT41

TIME: 03 Hours

Max. Marks: 100

Note: Answer any FIVE full questions, choosing at least ONE question from each module.

Q.No.	Question	M	L	CO	
Module -1					
01	a	Define Analytic function and hence derive C-R equations in Polar form.	06	L2	CO1
	b	Show that $w = f(z) = z + e^z$ is analytic and hence find its derivative.	07	L3	CO1
	c	Evaluate $\int_{(0,3)}^{(2,4)} (2y + x^2) dx + (3y - x) dy$ along with the parabola $x = 2t, y = t^2 + 3$.	07	L2	CO1
OR					
02	a	Find analytic function $f(z) = u + iv$ where $u - v = (x - y)(x^2 + 4xy + y^2)$ by the Milne-Thomson method.	06	L3	CO1
	b	State and prove Cauchy's integral formula.	07	L3	CO1
	c	Evaluate $\int_C \frac{e^{2z}}{(z+1)(z+2)} dz$, where C is a circle $ z = 3$.	07	L2	CO1
Module-2					
03	a	Show that $J_{-\frac{1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \cos x$	06	L2	CO2
	b	If α and β are two distinct roots of $J_n(x) = 0$, then prove that $\int_0^1 x J_n(\alpha x) J_n(\beta x) dx = 0.$	07	L2	CO2
	c	Show that $P_4(x) = \frac{1}{8}(35x^4 - 30x^2 + 3)$	07	L2	CO2
OR					
4	a	Show that $J_{-\frac{1}{2}}(x) = J_{\frac{1}{2}}(x) \cot x$	06	L2	CO2
	b	Find the series solution of the Legendre's equation $(1 - x^2) \frac{d^2 y}{dx^2} - 2x \frac{dy}{dx} + n(n+1)y = 0$, leading to Legendre polynomial of order n .	07	L2	CO2
	c	Express $4x^3 + 6x^2 + 7x + 2$ in terms of Legendre polynomials	07	L2	CO2
Module-3					

5	a	The following table gives the heights of father(x) and sons(y). Calculate the Karl Pearson's coefficient of correlation.	06	L2	CO3																		
<table border="1"> <tr> <td>x:</td> <td>65</td> <td>66</td> <td>67</td> <td>68</td> <td>68</td> <td>69</td> <td>70</td> <td>72</td> </tr> <tr> <td>y:</td> <td>67</td> <td>68</td> <td>65</td> <td>68</td> <td>72</td> <td>72</td> <td>69</td> <td>71</td> </tr> </table>			x:	65	66	67	68	68	69	70	72	y:	67	68	65	68	72	72	69	71			
x:	65	66	67	68	68	69	70	72															
y:	67	68	65	68	72	72	69	71															
	b	Fit a straight line $y = ax + b$ for the data	07	L2	CO3																		
<table border="1"> <tr> <td>x:</td> <td>12</td> <td>15</td> <td>21</td> <td>25</td> </tr> <tr> <td>y:</td> <td>50</td> <td>70</td> <td>100</td> <td>120</td> </tr> </table>			x:	12	15	21	25	y:	50	70	100	120											
x:	12	15	21	25																			
y:	50	70	100	120																			
	c	Using the method of least square, fit a curve $y = ax^b$ for the following data	07	L2	CO3																		
<table border="1"> <tr> <td>x:</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>y:</td> <td>2.98</td> <td>4.26</td> <td>5.21</td> <td>6.1</td> <td>6.8</td> <td>7.5</td> </tr> </table>			x:	1	2	3	4	5	6	y:	2.98	4.26	5.21	6.1	6.8	7.5							
x:	1	2	3	4	5	6																	
y:	2.98	4.26	5.21	6.1	6.8	7.5																	

OR

6	a	The scores for 9 students in Physics (x) and Mathematics (y) are as follows	06	L2	CO3																				
<table border="1"> <tr> <td>x:</td> <td>35</td> <td>23</td> <td>47</td> <td>17</td> <td>10</td> <td>43</td> <td>9</td> <td>6</td> <td>28</td> </tr> <tr> <td>y:</td> <td>30</td> <td>33</td> <td>45</td> <td>23</td> <td>8</td> <td>49</td> <td>12</td> <td>4</td> <td>31</td> </tr> </table> <p>Compute the Ranks and Rank correlation.</p>			x:	35	23	47	17	10	43	9	6	28	y:	30	33	45	23	8	49	12	4	31			
x:	35	23	47	17	10	43	9	6	28																
y:	30	33	45	23	8	49	12	4	31																
	b	Compute the means \bar{x} , \bar{y} and the correlation coefficient r from the given regression lines $4x - 5y + 33 = 0$, $20x - 9y = 107$	07	L2	CO3																				
	c	Fit a second-degree polynomial $y = ax^2 + bx + c$ for the data.	07	L2	CO3																				
<table border="1"> <tr> <td>x:</td> <td>20</td> <td>60</td> <td>100</td> <td>140</td> <td>180</td> <td>220</td> </tr> <tr> <td>y:</td> <td>0.18</td> <td>0.37</td> <td>0.35</td> <td>0.78</td> <td>0.56</td> <td>0.75</td> </tr> </table>			x:	20	60	100	140	180	220	y:	0.18	0.37	0.35	0.78	0.56	0.75									
x:	20	60	100	140	180	220																			
y:	0.18	0.37	0.35	0.78	0.56	0.75																			

Module-4

7	a	A random variable X has the following probability function:	06	L2	CO4																		
<table border="1"> <tr> <td>X</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> </tr> <tr> <td>P(X)</td> <td>0</td> <td>k</td> <td>2k</td> <td>2k</td> <td>3k</td> <td>k²</td> <td>2k²</td> <td>7k² + k</td> </tr> </table> <p>Find k. Also find $P(X < 6)$, $P(X \geq 6)$, $P(3 < X \leq 6)$.</p>			X	0	1	2	3	4	5	6	7	P(X)	0	k	2k	2k	3k	k ²	2k ²	7k ² + k			
X	0	1	2	3	4	5	6	7															
P(X)	0	k	2k	2k	3k	k ²	2k ²	7k ² + k															
	b	Derive the mean and variance of Poisson distribution.	07	L2	CO4																		
	c	The number of telephonic lines busy at an instant line is a binomial variate with a probability 0.1. If 10 lines are chosen at random, what is the probability that (i) No line is busy (ii) All lines are busy (iii) At least one line is busy	07	L3	CO4																		

OR

8	a	The diameter of a electric cable is assumed to be a continuous random variable with p.d.f $f(x) = \begin{cases} kx(1-x), & 0 \leq x < 1 \\ 0, & \text{else where} \end{cases}$ Find the value of k and also obtain the mean and variance of the variable	06	L2	CO4
	b	The number of accidents in a year to taxi drivers in a city follows a Poisson distribution with mean 3. Out of 1000 taxi drivers find approximately the number of drivers with i) No accident in a year ii) More than three accidents in a year.	07	L2	CO4
	c	If the life time of a certain types electric bulbs of a particular brand was distributed normally with an average life of 2000 hours and S.D.60 hours. If a firm purchase 2500 bulbs, find the number of bulbs that are likely to last for (i) More than 2100 hours (ii) Less than 1950 hours (iii) Between 1900 and 2100 hours.	07	L2	CO4

Module-5

9	a	The joint distribution of two random variables X and Y is as follows. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">Y X \</td> <td style="text-align: center;">1</td> <td style="text-align: center;">3</td> <td style="text-align: center;">6</td> </tr> <tr> <td style="text-align: center;">1</td> <td style="text-align: center;">$\frac{1}{9}$</td> <td style="text-align: center;">$\frac{1}{6}$</td> <td style="text-align: center;">$\frac{1}{18}$</td> </tr> <tr> <td style="text-align: center;">3</td> <td style="text-align: center;">$\frac{1}{6}$</td> <td style="text-align: center;">$\frac{1}{4}$</td> <td style="text-align: center;">$\frac{1}{12}$</td> </tr> <tr> <td style="text-align: center;">6</td> <td style="text-align: center;">$\frac{1}{18}$</td> <td style="text-align: center;">$\frac{1}{12}$</td> <td style="text-align: center;">$\frac{1}{36}$</td> </tr> </table> Compute the following. i) Marginal distributions of X and Y ii) Are X and Y stochastically independent?	Y X \	1	3	6	1	$\frac{1}{9}$	$\frac{1}{6}$	$\frac{1}{18}$	3	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{12}$	6	$\frac{1}{18}$	$\frac{1}{12}$	$\frac{1}{36}$	06	L2	CO5
Y X \	1	3	6																		
1	$\frac{1}{9}$	$\frac{1}{6}$	$\frac{1}{18}$																		
3	$\frac{1}{6}$	$\frac{1}{4}$	$\frac{1}{12}$																		
6	$\frac{1}{18}$	$\frac{1}{12}$	$\frac{1}{36}$																		
	b	A set of five similar coins is tossed 320 times and the result is <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td style="text-align: center;">No. of heads</td> <td style="text-align: center;">0</td> <td style="text-align: center;">1</td> <td style="text-align: center;">2</td> <td style="text-align: center;">3</td> <td style="text-align: center;">4</td> <td style="text-align: center;">5</td> </tr> <tr> <td style="text-align: center;">Frequency</td> <td style="text-align: center;">6</td> <td style="text-align: center;">27</td> <td style="text-align: center;">72</td> <td style="text-align: center;">112</td> <td style="text-align: center;">71</td> <td style="text-align: center;">32</td> </tr> </table> Test the hypothesis that the data follows a binomial distribution at 5% significance level	No. of heads	0	1	2	3	4	5	Frequency	6	27	72	112	71	32	07	L2	CO5		
No. of heads	0	1	2	3	4	5															
Frequency	6	27	72	112	71	32															
	c	A certain stimulus administered to each of the 12 patients resulted in the following change in the blood pressure 5, 2, 8, -1, 3, 0, 6, -2, 1, 5, 0, 4. Can it be concluded that the stimulus will increase the blood pressure? (Note : $t_{0.05}$ for 11 d.f. is 2.201).	07	L3	CO5																

OR																				
10	a	Determine (i) Marginal distributions (ii) Correlation coefficient between the variables X and Y , from the joint probability distribution given by:	06	L2	CO5															
		<table border="1"> <tr> <td>$Y \backslash X$</td> <td>-2</td> <td>-1</td> <td>4</td> <td>5</td> </tr> <tr> <td>1</td> <td>0.1</td> <td>0.2</td> <td>0</td> <td>0.3</td> </tr> <tr> <td>2</td> <td>0.2</td> <td>0.1</td> <td>0.1</td> <td>0</td> </tr> </table>	$Y \backslash X$	-2	-1	4	5	1	0.1	0.2	0	0.3	2	0.2	0.1	0.1	0			
$Y \backslash X$	-2	-1	4	5																
1	0.1	0.2	0	0.3																
2	0.2	0.1	0.1	0																
	b	The 9 item of a sample have the following values 45, 47, 50, 52, 48, 47, 49, 53, 51. Does the mean of these differ significantly from the assumed mean of 47.5? ($t_{0.05} = 2.306$ for 8 d.f.)	07	L3	CO5															
	c	The theory predicts the proportion of beans in the four groups A, B, C and D should be 9:3:3:1. In an experiment among 1600 beans, the number in the Four groups were 882, 313, 287 and 118. The goodness of fit χ^2 value of above data is approximately equal to?	07	L3	CO5															

Bloom's Taxonomy Levels	Lower-order thinking skills		
	Remembering (knowledge):L ₁	Understanding (Comprehension): L ₂	Applying (Application):L ₃
	Higher-order thinking skills		
	Analyzing (Analysis):L ₄	Valuating (Evaluation): L ₅	Creating (Synthesis): L ₆