

Model Question Paper-II with effect from 2022 (CBCS Scheme)

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Second Semester B.E Degree Examination

Mathematics-II for CIVIL ENGINEERING STREAM -BMATC201

TIME: 03 Hours

Max. Marks: 100

- Note:
1. Answer any **FIVE** full questions, choosing at least **ONE** question from each **module**.
 2. VTU Formula Hand Book is permitted.
 3. M: Marks, L: Bloom's level, C: Course outcomes.

Module -1			M	L	C
Q.01	a	Evaluate $\int_0^a \int_0^{\sqrt{a^2-x^2}} \int_0^{\sqrt{a^2-x^2-y^2}} \frac{1}{\sqrt{a^2-x^2-y^2-z^2}} dz dy dx$	7	L3	CO1
	b	Evaluate $\int_0^{4a} \int_{2\sqrt{ax}}^{\frac{x^2}{2\sqrt{ax}}} xy dy dx$ by changing the order of integration	7	L3	CO1
	c	Define beta and gamma functions. Show that $\gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$	6	L2	CO1
OR					
Q.02	a	Evaluate $\int_0^a \int_y^a \left(\frac{x^2}{(x^2+y^2)^{3/2}}\right) dx dy$ by changing into polar coordinates	7	L3	CO1
	b	Using double integration find the area enclosed between the parabola $y = x^2$ and the line $y = x$	7	L3	CO1
	c	Write a modern mathematical program to evaluate the integral $\int_0^3 \int_0^{3-x} \int_0^{3-x-y} (xyz) dz dy dx$	6	L3	CO5
Module-2					
Q.03	a	If $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ show that (i) $\nabla \cdot \vec{r} = 3$ (ii) $\nabla \times \vec{r} = \vec{0}$ and (iii) $\nabla r^n = nr^{n-2}\vec{r}$	7	L2	CO2
	b	If $\vec{F} = \nabla(xy^3z^2)$ find $div \vec{F}$ and $curl \vec{F}$ at the point $(1, -1, 1)$.	7	L2	CO2
	c	Define an irrotational vector. Find the constants a, b and c such that $\vec{A} = (axy - z^3)\hat{i} + (bx^2 + z)\hat{j} + (bxz^2 + cy)\hat{k}$ is irrotational.	6	L2	CO2
OR					
Q.04	a	Evaluate $\int (5xy - 6x^2)dx + (2y - 4x)dy$, over the curve $y = x^3$ in the xy -plane from the point $(1, 1)$ to $(2, 8)$	7	L2	CO2
	b	Use Stoke's theorem to evaluate $\int_C \vec{F} \cdot d\vec{r}$, where $\vec{F} = (x^2 + y^2)\hat{i} - 2xy\hat{j}$ and C is bounded by $x = \pm a, y = b$	7	L3	CO2

	c	Write a modern mathematical tool program to evaluate $\oint_c [(xy + y^2)dx + x^2dy]$, where c is the closed curve bounded by $y = x$ and $y = x^2$ by using Green's theorem.	6	L3	C05												
Module-3																	
Q. 05	a	Form the partial differential equation by eliminating the arbitrary function from the relation $lx + my + nz = f(x^2 + y^2 + z^2)$	7	L2	C03												
	b	Solve $\frac{\partial^2 z}{\partial x^2} = xy$, subject to the conditions $\frac{\partial z}{\partial x} = \log(1 + y)$, when $x = 1$ and $z = 0$, when $x = 0$.	7	L3	C03												
	c	With usual notations derive a one-dimensional heat equation	6	L2	C03												
OR																	
Q. 06	a	Form the partial differential equation by eliminating the arbitrary constants from $(x - a)^2 + (y - b)^2 + z^2 = 4$	7	L2	C03												
	b	Solve $\frac{\partial^2 z}{\partial y^2} = z$, given that when $y = 0, z = e^x$ and $\frac{\partial z}{\partial y} = e^{-x}$	7	L3	C03												
	c	Solve $x^2(y - z)p + y^2(z - x)q = z^2(x - y)$	6	L3	C03												
Module-4																	
Q. 07	a	By Newton's-Raphson method find the root of $x \sin x + \cos x = 0$ which is near to $x = \pi$	7	L3	C04												
	b	Using Lagrange's interpolation formula, fit a polynomial which passes through the points $(-1, 0)$, $(1, 2)$, $(2, 9)$ and $(3, 8)$ and hence estimate the value of y when $x = 2.2$	7	L3	C04												
	c	Evaluate $\int_4^{5.2} \log x dx$ using Simpson's (3/8)th rule by taking 7 ordinates	6	L3	C04												
OR																	
Q. 08	a	Find an approximate value of the root of the equation $xe^x = 3$, using the method of false position, carry out four iterations.	7	L3	C04												
	b	The population of a town is given by the following table: <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td>Year</td> <td>1951</td> <td>1961</td> <td>1971</td> <td>1981</td> <td>1991</td> </tr> <tr> <td>Population</td> <td>19.6</td> <td>39.65</td> <td>58.81</td> <td>72.21</td> <td>94.61</td> </tr> </tbody> </table> Using Newton's forward and backward interpolation formula, calculate the increase in population between the years 1955 and 1985.	Year	1951	1961	1971	1981	1991	Population	19.6	39.65	58.81	72.21	94.61	7	L3	C04
Year	1951	1961	1971	1981	1991												
Population	19.6	39.65	58.81	72.21	94.61												
	c	Evaluate $\int_0^{0.3} (1 - 8x^3)^{\frac{1}{2}} dx$ by using Simpson's $\left(\frac{1}{3}\right)^{rd}$ rule, by taking 3 equal intervals.	6	L3	C04												
Module-5																	
Q. 09	a	Use Taylor's series method to find $y(0.2)$ from $\frac{dy}{dx} = x^2y - 1$, with $y(0) = 1$	7	L3	C04												
	b	Using Runge-Kutta method of order 4, find y at $x = 0.1$, given that $\frac{dy}{dx} = 3e^x + 2y$, $y(0) = 1$	7	L3	C04												

	c	Applying Milne's Predictor-Corrector method , find $y(0.8)$, from $\frac{dy}{dx} = x^3 + y$, given that $y(0) = 2$, $y(0.2) = 2.073$, $y(0.4) = 2.452$, $y(0.6) = 3.023$	6	L3	CO4
OR					
Q. 10	a	Solve by Using Modified Euler's method, $y' = \log_{10}(x + y)$, $y(0) = 2$ at $x = 0.2$ and $x = 0.4$	7	L3	CO4
	b	Find the value of $y(0.5)$ using the Runge-Kutta method of fourth order, for the given equation $(x + y) \frac{dy}{dx} = 1$; $y(0.4) = 1$	7	L3	CO4
	c	Write a modern mathematical tool program to solve $y' + 4y = x^2$ with initial conditions $y(0) = 1$ using Taylor's series method at $x = 0.1, 0.2$	6	L3	CO5

Bloom's Taxonomy Levels	Lower-order thinking skills		
	Remembering (knowledge):L ₁	Understanding (Comprehension): L ₂	Applying (Application): L ₃
	Higher-order thinking skills		
	Analyzing (Analysis):L ₄	Valuating (Evaluation): L ₅	Creating (Synthesis): L ₆

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 2. VTU Formula Hand Book is permitted.
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Module -1			M	L	C
Q.01	a	Evaluate $\int_0^1 \int_{y^2}^1 \int_0^{1-x} x \, dz \, dx \, dy$	7	L3	CO1
	b	Evaluate $\int_0^a \int_y^a \frac{x}{x^2+y^2} \, dx \, dy$ by changing the order of integration	7	L3	CO1
	c	Derive the relation $\beta(m, n) = \frac{\gamma(m) \gamma(n)}{\gamma(m+n)}$	6	L2	CO1
OR					
Q.02	a	Evaluate $\int_0^1 \int_0^{\sqrt{1-y^2}} (x^2 + y^2) \, dx \, dy$ by changing into polar coordinates	7	L3	CO1
	b	Using double integration find the area of a plate in the form of a quadrant of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$	7	L3	CO1
	c	Write a modern mathematical tool program to evaluate the double integral $\int_0^1 \int_0^x (x^2 + y^2) \, dy \, dx$	6	L3	CO5
Module-2					
Q.03	a	Find the directional derivative of $\phi = x^2yz + 4xz^2$ at the point $(1, -2, 1)$ in the direction of the vector $2\hat{i} - \hat{j} - 2\hat{k}$	7	L2	CO2
	b	Evaluate $Curl(Curl\vec{F})$ and $div(curl\vec{F})$, If $\vec{F} = x^2y\hat{i} + y^2z\hat{j} + z^2x\hat{k}$	7	L3	CO2
	c	Show that $\vec{F} = (y^2 - z^2 + 3yz - 2x)\hat{i} + (3xz + 2xy)\hat{j} + (3xy - 2xz + 2z)\hat{k}$ is both solenoidal and irrotational	6	L2	CO2
OR					
Q.04	a	Find the work done in moving a particle in the force field $\vec{F} = 3x^2\hat{i} + (2xz - y)\hat{j} + z\hat{k}$ along the straight line from $(0, 0, 0)$ to $(2, 1, 3)$	7	L2	CO2
	b	Using Green's theorem, Evaluate $\oint[(3x - 8y^2)dx + (4y - 6xy)dy]$ over the boundary of the region $x = 0, y = 0, \text{ and } x + y = 1$	7	L3	CO2
	c	Write a modern mathematical tool program to find the gradient of $\phi = x^2y + 2xz - 4$	6	L3	CO5
Module-3					
Q.05	a	Form the partial differential equation from the relation $z = f(x + at) + g(x - at)$	7	L2	CO3

	b	Solve $\frac{\partial^2 z}{\partial x \partial y} = \sin x \sin y$ for which $\frac{\partial z}{\partial y} = -2 \sin y$ when $x = 0$ and $z = 0$ when y is an odd multiple of $\frac{\pi}{2}$.	7	L3	C03														
	c	Solve $x(y^2 - z^2)p + y(z^2 - x^2)q - z(x^2 - y^2)r = 0$	6	L3	C03														
OR																			
Q. 06	a	Form the partial differential equation from $f(x + y + z, x^2 + y^2 + z^2) = 0$	7	L2	C03														
	b	Solve $\frac{\partial^2 z}{\partial x^2} + \frac{\partial z}{\partial x} - 4z = 0$, given that when $x = 0, z = 1$ and $\frac{\partial z}{\partial x} = y$	7	L3	C03														
	c	With usual notations, derive one-dimensional wave equation $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$	6	L2	C03														
Module-4																			
Q. 07	a	Find a real root of $x^3 - 9x + 1 = 0$ in $(2, 3)$ by the Regula-Falsi method in four iterations.	7	L3	C04														
	b	Using Newton's forward interpolation find y at $x = 5$ from the data <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td style="text-align: center;">x</td> <td style="text-align: center;">4</td> <td style="text-align: center;">6</td> <td style="text-align: center;">8</td> <td style="text-align: center;">10</td> </tr> <tr> <td style="text-align: center;">y</td> <td style="text-align: center;">1</td> <td style="text-align: center;">3</td> <td style="text-align: center;">8</td> <td style="text-align: center;">16</td> </tr> </tbody> </table>	x	4	6	8	10	y	1	3	8	16	7	L3	C04				
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OR																			
Q. 08	a	Find the real root of the equation $\cos x = xe^x$, which is nearer to $x = 0.5$ by the Newton-Raphson method, correct to four decimal places.	7	L3	C04														
	b	Determine $f(x)$ as a polynomial in x for the data given below by using Newton's divided difference formula <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td style="text-align: center;">x</td> <td style="text-align: center;">2</td> <td style="text-align: center;">4</td> <td style="text-align: center;">5</td> <td style="text-align: center;">6</td> <td style="text-align: center;">8</td> <td style="text-align: center;">10</td> </tr> <tr> <td style="text-align: center;">f(x)</td> <td style="text-align: center;">10</td> <td style="text-align: center;">96</td> <td style="text-align: center;">196</td> <td style="text-align: center;">350</td> <td style="text-align: center;">868</td> <td style="text-align: center;">1746</td> </tr> </tbody> </table>	x	2	4	5	6	8	10	f(x)	10	96	196	350	868	1746	7	L3	C04
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Q. 09	a	Find an approximate value of y when $x = 0.1$, if $\frac{dy}{dx} = x - y^2$ and $y = 1$ at $x = 0$ using Taylor's series method.	7	L3	C04														
	b	Given $\frac{dy}{dx} = \frac{y-x}{y+x}$ with the initial condition $y = 1$ when $x = 0$. Find approximately y for $x = 0.1$ by Modified Euler's method. Carry out three modifications.	7	L3	C04														

	c	Given $\frac{dy}{dx} = xy + y^2$, $y(0) = 1$, $y(0.1) = 1.1169$, $y(0.2) = 1.2773$, $y(0.3) = 1.5049$, compute $y(0.4)$ using Milne's Predictor-Corrector method.	6	L3	CO4
OR					
Q. 10	a	Using modified Euler's formula, compute $y(1.1)$ correct to three decimal places given that $\frac{dy}{dx} + \frac{y}{x} = \frac{1}{x^2}$ and $y = 1$ at $x = 1$.	7	L3	CO4
	b	Using the Runge-Kutta method of fourth order solve $\frac{dy}{dx} = \frac{y^2 - x^2}{y^2 + x^2}$ with $y(0) = 1$ at $x = 0.2$	7	L3	CO4
	c	Write a modern mathematical tool program to solve $\frac{dy}{dx} = 2x + y$, $y(1) = 2$ by the Runge-Kutta 4 th order method.	6	L3	CO5

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	Higher-order thinking skills		
	Analyzing (Analysis):L ₄	Valuating (Evaluation): L ₅	Creating (Synthesis): L ₆