

GBCS SCHEME

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18ME733

Seventh Semester B.E. Degree Examination, Feb./Mar. 2022 Computational Fluid Dynamics

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. What is the need of a CFD tool? Elaborate on two applications of CFD in detail. (04 Marks)
- b. What is a substantial derivative? Write an expression for the substantial derivative of velocity. (06 Marks)
- c. Derive the Navier-Stokes equation (PDE form) in the Cartesian coordinate system. (10 Marks)

OR

- 2 a. Write a short note on gradient, divergence and curl operators. (06 Marks)
- b. Explain the mathematical classification of second order PDE's with examples. (06 Marks)
- c. Derive the integral form of Navier-Stokes equation from PDE's. (08 Marks)

Module-2

- 3 a. Explain the conserved and primitive variables. (04 Marks)
- b. Obtain the eigen values and eigen vectors of gas dynamics equation as given below:

$$\frac{\partial \rho}{\partial t} + \rho_0 \frac{\partial u}{\partial x} = 0$$

$$\frac{\partial u}{\partial t} + \frac{a^2}{\rho_0} \frac{\partial \rho}{\partial x} = 0$$

ρ_0 = constant reference density

a = sound speed

- c. Derive the Reynolds averaged momentum equations. (10 Marks)

OR

- 4 a. With the help of a telescoping series, write the conservative and non conservative forms of the following derivative and explain the significance of boundary terms.

$$\frac{\partial \rho u}{\partial x}$$

Consider a one-dimensional domain which is spatially discretized using three elements and four nodes. How to choose the scheme (conservative and non conservative) for a given fluid flow? (06 Marks)

- b. Explain the terms: (i) turbulent kinetic energy (ii) dissipation rate (04 Marks)
- c. Derive the conservative form of the Navier-Stokes equation from its non conservative form. (10 Marks)

Module-3

- 5 a. Find $\langle f, g \rangle$, $\|f\|$ and $\|g\|$ for the following functions on the interval $(-1, 1)$, $f(x) = x^2$ and $g(x) = x^3$. (04 Marks)
- b. What is a representation error? (04 Marks)

- c. Using box function, find the representations for the following function on the interval $x \in [0, 1]$ $p(x) = x = p_f f + p_g g + p_h h$
Use four nodes $\left\{0.0, \frac{1}{3}, \frac{2}{3}, 1.0\right\}$. Find the error in the representations. (12 Marks)

OR

- 6 a. On the interval of $[-1, 1]$, find the angle between the functions $f(x) = 1$ and $g(x) = x$. How about if the interval considered is $[0, 1]$? (06 Marks)
b. With the necessary equations, explain linear approximation using Hat functions. With the help of schematics, explain the representation of $\sin(\pi x)$ using five nodes on the interval $[0, 1]$. (10 Marks)
c. With necessary equations, explain machine epsilon. (04 Marks)

Module-4

- 7 a. Compute forward, backward and central difference approximations for the first derivative of $f(x) = \frac{3x+5}{x-4}$ at $x = 2$. Use a step size of 0.01. Compare these values with the exact values and comment on your calculations. (10 Marks)
b. Explain the explicit and implicit approaches as applied to linear convection equations. (10 Marks)

OR

- 8 a. Why iterative methods are preferred in numerical methods. Differentiate Jacobi and Gauss-Siedel iterative methods. (08 Marks)
b. Describe the First Order Forward Time and Centered Space (FTCS) method of solving one dimensional transient diffusion equation
$$\frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2}$$
where D is the diffusion coefficient. (08 Marks)
c. Discuss the upwind scheme in finite difference method. (04 Marks)

Module-5

- 9 a. State the disadvantages of Lax-Wendroff technique and explain MacCormack's technique. (10 Marks)
b. Describe the Flux Splitting Method. (05 Marks)
c. Write a short note on Finite Volume Method. (05 Marks)

OR

- 10 a. Derive the MacCormack scheme for two-dimensional time dependent compressible flow. (10 Marks)
b. Compare the finite volume flux splitting for the Euler equation using:
(i) Steger and Warming Method
(ii) Roe's Method (10 Marks)

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