

Sixth Semester B.Tech. Degree Examination, June/July 2023

Finite Element Method

Time: 3 hrs.

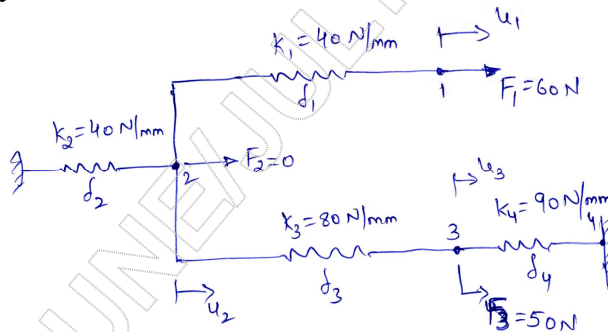
Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. Write the equations of equilibrium and strain displacement equation for 3D elastic problem. (10 Marks)
- b. For the spring shown in Fig.Q.1(b). Determine the nodal displacement using principle of minimum potential energy. (10 Marks)

Fig.Q.1(b)



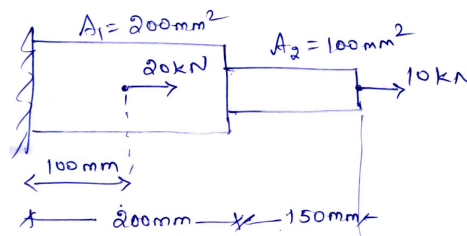
OR

- 2 a. Explain Rayleigh Ritz method for FEM. (10 Marks)
- b. Explain the types of FEM elements. List the applications of FEM. (10 Marks)

Module-2

- 3 a. Using direct stiffness method, determine the nodal displacement of stepped bar as shown in Fig.Q.3(a). Also determine reaction support, stresses in each element. Take $E = 200\text{GPa}$. (10 Marks)

Fig.Q.3(a)

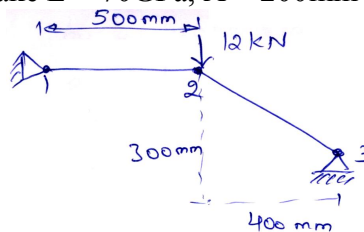


- b. Derive the stiffness matrix in trusses. (10 Marks)

OR

- 4 a. For the 2 bar truss as shown in Fig.Q.4(a). Determine the displacement at node 2 and stresses in both the elements. Take $E = 70\text{GPa}$, $A = 200\text{mm}^2$. (10 Marks)

Fig.Q.4(a)

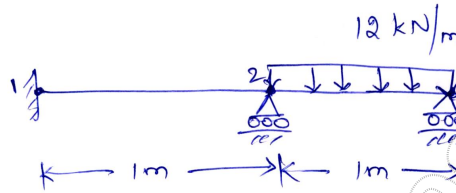


- b. Derive stiffness matrix for spring element. (10 Marks)

Module-3

- 5 a. Derive the stiffness matrix for beams. (10 Marks)
 b. For the beam shown in Fig.Q.5(b). Determine:
 i) Slope at node
 ii) Vertical deflection at mid point of distributed load.
 Take $E = 200\text{GPa}$, $I = 4 \times 10^6\text{mm}^4$.

Fig.Q.5(b)



(10 Marks)

OR

- 6 a. Derive the equation for Hermite shape function. (10 Marks)
 b. A beam fixed at one end and supported by a roller at the other end has a 20kN concentrated load applied at the center of the span as shown in Fig.Q.6(b). Calculate the deflection under the load. Take $E = 20 \times 10^6\text{N/cm}^2$, $I = 2500\text{cm}^4$. (10 Marks)

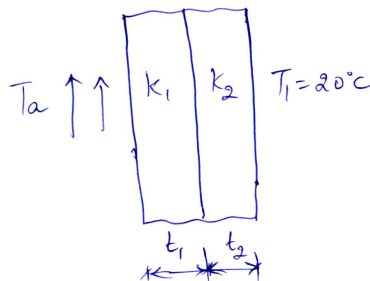
Module-4

- 7 a. A composite slab consists of three materials with thermal conductivity of $20\text{W/m}^\circ\text{C}$, $30\text{W/m}^\circ\text{C}$, $50\text{W/m}^\circ\text{C}$ and thickness 0.3m , 0.15m and 0.15m respectively. The outer surface is at 20°C and the inner surface is exposed to the convective heat transfer coefficient of $25\text{W/m}^2^\circ\text{C}$ and a medium at 800°C . Determine the temperature distribution within the wall. (10 Marks)
 b. Write the rate equations for conduction, convection and radiation. (10 Marks)

OR

- 8 a. Determine the temperature distribution through the composite wall shown in Fig.Q.8(a) when the convection heat loss occurs on the left surface. Assume unit area. Assume wall thickness $t_1 = 4\text{cm}$, $t_2 = 2\text{cm}$, $k_1 = 0.5\text{W/cm}^\circ\text{C}$, $k_2 = 0.05\text{W/cm}^\circ\text{C}$, $h = 0.1\text{W/cm}^2^\circ\text{C}$ and $T_a = -5^\circ\text{C}$. (10 Marks)

Fig.Q.8(a)



- b. Write a note on fluid flow through porous medium and its analysis through FEM.

(10 Marks)

Module-5

- 9 a. Define Axisymmetric solid. Write the equation of equilibrium. (10 Marks)
 b. Write a note on consistent element mass matrix of one dimensional bar element. (10 Marks)

OR

- 10 a. Explain the formulation of point mass and distributed masses. (10 Marks)
 b. Write a note on lumped mass matrix of bar element. (10 Marks)